

UNIT-I

GROUP - I

TOPIC - RELATION

1 MARKS QUESTION

1. If A & B are any two non-empty sets, then a subset of $A \times B$ is called
2. If $(x, x) \in R$ for each element $x \in A$ then the relation R in A is
3. If $x R y \Rightarrow y R x \forall x, y \in A$, then the relation R in A is.....
4. If $(x, y) \in R$ and $(y, z) \in R \forall x, y, z \in A$ then the relation R in A is.....
5. Write the domain of the Relation
 $R = \{(-1, 1), (1, 1), (2, 4), (-3, 5)\}$
6. Find the range of relation
 $R = \{(2, 3), (-1, 2), (0, 1), (4, 5)\}$
7. If $r = \left\{ X, \frac{1}{X} \right\} : x \in \mathbb{N} \text{ and } 1 \leq x \leq 4$. List the elements of R.
8. If $A = \{1, 2\}$. How many equivalence relation on set A is possible ?
9. The relation $R : \{1, 2, 3\} \rightarrow \{1, 2, 3\}$ given by $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3)\}$ is
10. If $A = \{a, b, c\}$ and R is a relation in A given by
 $R = \{(a, a), (a, b), (a, c), (b, a), (c, a)\}$
Whether R is symmetric or not.
11. Whether the relation R in the set $\{1, 2, 3\}$ given by $R = \{(1, 2), (2, 1)\}$ is transitive or not.
12. The relation R in the set A of human beings in a town at a particular time is given by
 $R = \{(x, y) \in A \times A : x \text{ is brother of } y\}$. Is it symmetric ?
13. If $A = \{1, 2, 3, 4, 6\}$ and let R be a relation on A defined by
 $R = \{(a, b) : a \in A, b \in A \text{ and } a \text{ divides } b\}$. List the elements of R.
14. Let $R = \{(a, a^3) : a \text{ is a prime number less than } 10\}$. Find R.
15. If R_1 and R_2 are reflexive relation in a set A, then $R_1 \cap R_2$ is..... relation.
16. If $A = \{1, 3, 5\}$, $B = \{9, 11\}$ and let $R = \{(a, b) \in A \times B : a - b \text{ is odd}\}$. Write the relation R.
17. If $A = \{a, b, c\}$. How many equivalence relation on the set A is possible.
18. The relation R in the set A of human beings in a town at a particular time given by
 $R = \{(x, y) : x \text{ and } y \text{ work at the same place}\}$ of what type ?
19. If $A = \{3, 5, 7\}$ and $B = \{2, 4, 9\}$ and R is a relation from A to B given by $a \leq b$ for all $a \in A$ and $b \in B$.
write R as a set of ordered pair.
20. How many number of equivalence relations are there on the set $\{3, 4, 5\}$ containing $\{3, 4\}$ and $\{4, 3\}$?

4 MARKS QUESTIONS

1. Let L be the set of all lines in a plane and R be the relation in L defined as $R = \{(L_1, L_2) : L_1 \text{ is perpendicular to } L_2\}$. Show that R is symmetric but not transitive.
2. Show that the relation R in the set $A = \{1, 2, 3, 4, 5, 6\}$. Defined as $R = \{(x, y) : y \text{ is divisible by } x\}$ is (i) transitive (ii) not symmetric.
3. Let R be the relation in the set $A = \{1, 2, 3, 4\}$ - defined by $R = \{(1, 2), (2, 2), (1, 1), (4, 4), (1, 3), (3, 3), (3, 2)\}$. Show that R is (i) reflexive (ii) transitive
4. Show that the relation $R = \{a, b\} : a > b\}$ on \mathbb{N} is (i) transitive (ii) not reflexive
5. On the set S of all real numbers. Define a relation $R = \{(a, b) : 1 + ab > 0\}$. Show that R is (i) reflexive (ii) not transitive
6. On the set of all real numbers, define a relation $R = \{a, b\} : a < b^2\}$. Show that R is (i) not symmetric (ii) not transitive
7. Let $A = \{1, 2, 3, 4, 5, 6\}$. Consider a relation R on A, defined by $R = \{(a, b) : b = a + 1\}$. Show that R

- is (i) not symmetric (ii) not transitive
8. Show that the relation R in the set $\{1,2,3\}$ given by $R = \{(1, 1),(2,2),(3,3),(1,2),(2,3)\}$ is (i) not symmetric (ii) not reflexive
 9. Give an example of a relation which is (i) symmetric (ii) not transitive
 10. Give an example of a relation which is (i) symmetric (ii) not reflexive
 11. Give an example of a relation which is (i) transitive (ii) not reflexive
 12. Show that the relation R in \mathbf{R} defined as $R=\{(a,b) : a \leq b\}$ is (i)transitive (ii)not transitive
 13. Show that the relation R on a set $A= \{1,2,3,4,\dots\dots\dots,14\}$ defined as $R=\{(x,y) :3x-y=0\}$ is neither reflexive nor symmetric
 14. Show that the relation R in the set N of natural number defined as $R= \{(x, y):y=x+5 \text{ and } x <4\}$ is (i) not reflexive (ii) transitive
 15. Give an example of a relation which is (i) reflexive (ii) transitive

6 MARKS QUESTIONS

1. Let A be the set of all lines in xy - plane and R be a relation in A, defined by $R = \{(L1, L2) : L1 \parallel L2\}$
Show that (i) R is reflexive
(ii) R is symmetric
(iii) R is transitive
(iv) Find the set of all lines related to the line $y = 3x + 5$
2. Show that the relation R in the set $A = \{x \in \mathbf{Z} : 0 \leq x \leq 12\}$ given by $R = \{(a, b) : |a - b| \text{ is a multiple of } 4\}$ is
(i) reflexive
(ii) symmetric
(iii) transitive
(iv) Find the set of all elements related to 1
3. Let s be the set of all points in a plane and let R be a relation in s defined by $R = \{(A, B) : \delta(A, B) < 2 \text{ units}\}$, where $\delta(A, B)$ is the distance between points A & B.
Show that (i) R is reflexive
(ii) R is symmetric
(iii) R is not transitive
4. Let $R = \{(a, b) : a, b \in \mathbf{Z} \text{ and } (a-b) \text{ is divisible by } 5\}$. Show that R is an equivalence relation on \mathbf{Z} .
5. Show that the relation R defined in the set A of all polygons as $R = \{(P1, P2) : P1 \text{ \& } P2 \text{ have same number of sides}\}$ is an equivalence relation. What is the set of all elements in A related to the right angle triangle T with sides 3, 4 and 5 ?
6. Let N be the set of all natural number and let R be a relation on $\mathbf{N} \times \mathbf{N}$ defined by $(a, b) R (c, d) \iff ad = bc$
Show that R is an equivalence relation.
7. Show that the relation R on $\mathbf{N} \times \mathbf{N}$ defined by $(a, b) R (c, d) \iff a + d = b + c$ is an equivalence relation.
8. Let A be the set of all triangles in a plane. Show that the relation $R = \{(\Delta1, \Delta2) : \Delta1 \sim \Delta2\}$ is an equivalence relation.
9. show that the relation R in the set $A = \{1,2,3,4, 5\}$ given by $R = \{(a, b) : |a - b| \text{ is even}\}$ is an equivalence relation.
10. Show that the relation R in the set Z of integers given by $R = \{(a, b) : 2 \text{ divides } a - b\}$ is an equivalence relation.
Or
Let $R = \{(a,b) : a = b^2, a, b \in \mathbf{N}\}$
Show that (i) R is not reflexive
(ii) R is not symmetric
(iii) R is not transitive